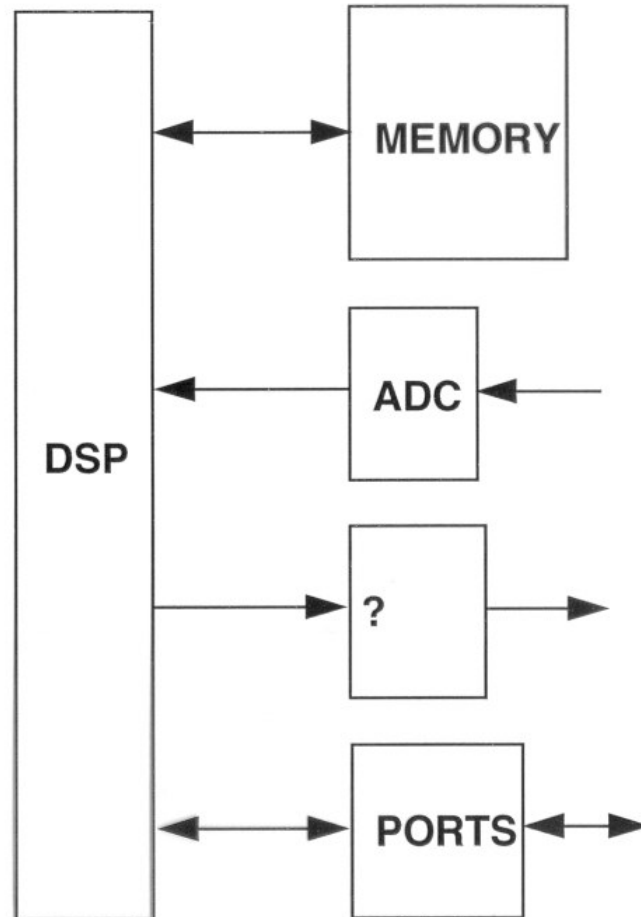


A TYPICAL DSP SYSTEM

Typické usporiadanie systému „Digital Signal Processor“



- **DSP CHIP** Číslicový signálový procesor
- **MEMORY**
- **CONVERTERS (OPTIONAL)** Prevodníky (voliteľná súčasť)
 - ANALOGUE TO DIGITAL
 - DIGITAL TO ANALOGUE
- **COMMUNICATION PORTS**
 - SERIAL
 - PARALLEL

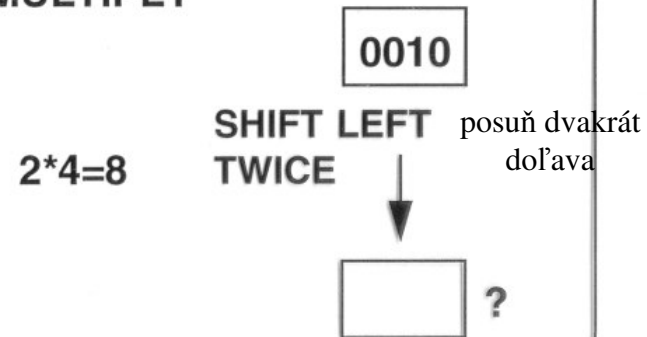
MULTIPLY AND ADD

Operácie násobenia (Multiply) a sčítania (Add)

ADD

$$\begin{array}{r}
 1+2=3 \\
 + \\
 \hline
 \end{array}
 \begin{array}{r}
 0001 \\
 0010 \\
 \hline
 0011
 \end{array}$$

MULTIPLY



Najviac používaná operácia v DSP
MOST COMMON OPERATION IN DSP

$$A = B * C + D$$

$$E = F * G + A$$

⋮

MULTIPLY, ADD AND ACCUMULATE

MAC INSTRUCTION

násob a výsledok pričítaj k predošlému
 výsledku (operand A)

MULTIPLY OPERATION

**TYPICALLY 70 CLOCK CYCLES
 WITH ORDINARY PROCESSORS**
 v bežnom mikroradiči trvá výpočet násobenia
 až 70 strojových cyklov

WE NEED TO MAC IN ONE CYCLE

My ale potrebujeme násobiť a pripočítavať v

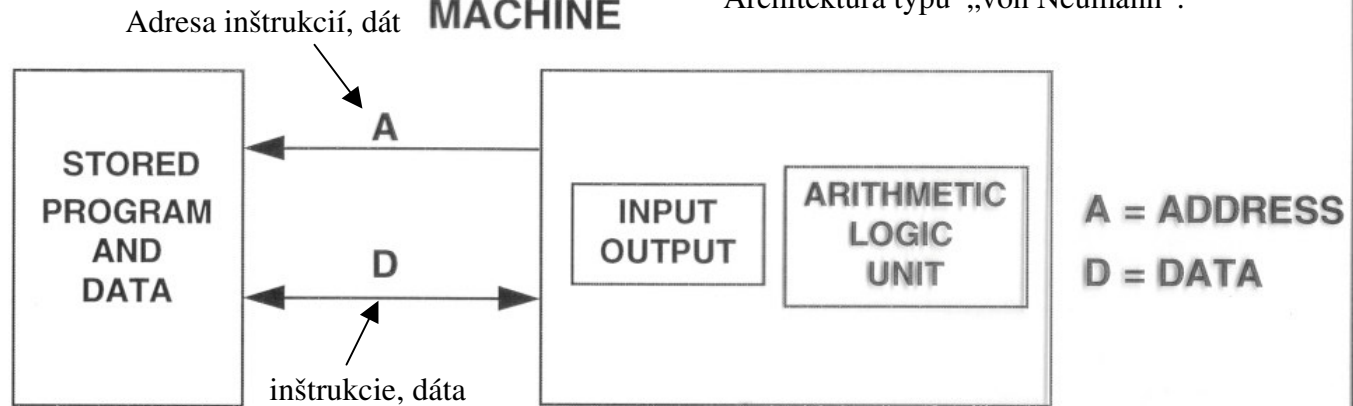
JEDNOM strojovom cykle

DIGITAL COMPUTERS

Procesory - dve architektúry:

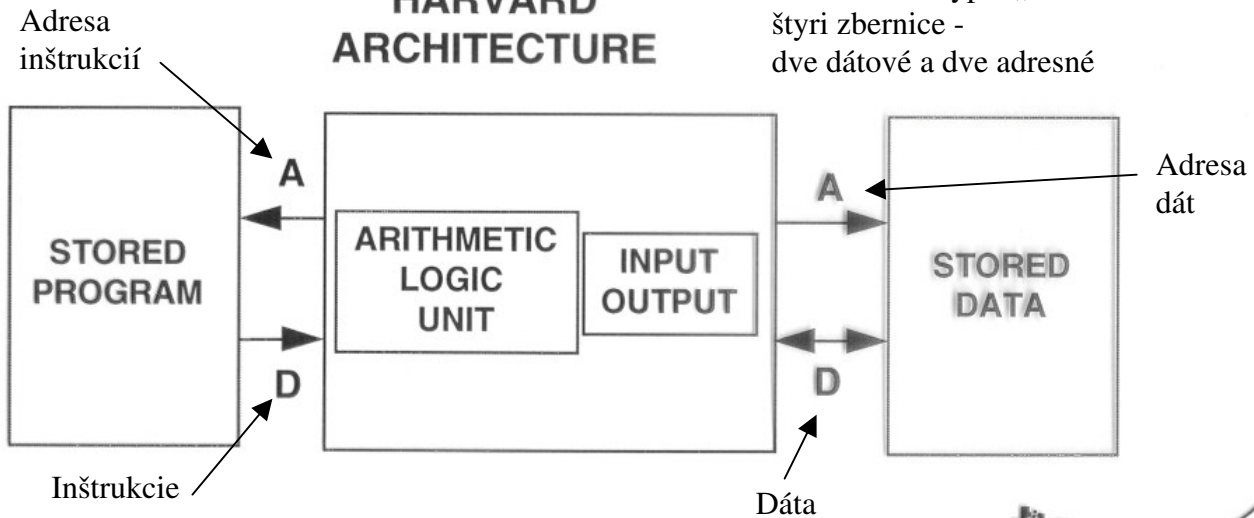
VON NEUMAN MACHINE

Architektúra typu „von Neumann“:



HARVARD ARCHITECTURE

Architektúra typu „Harvard“:
štyri zbernice -
dve dátové a dve adresné



WHY DIGITAL?

Prečo číslicové spracovanie?

- IS IT WORTH IT?

Stojí to zato? Zaslúži si to?



- IS DIGITAL PROCESSING BETTER?

Je číslicové spracovanie výhodnejšie?

- APPLICATION DEPENDENT

Niekedy áno niekedy nie, závisí na aplikácii

- PROGRAMMABILITY

Programovateľnosť, zmena programu - zmena funkcie

- STABILITY AND REPEATABILITY

- SPECIAL APPLICATIONS

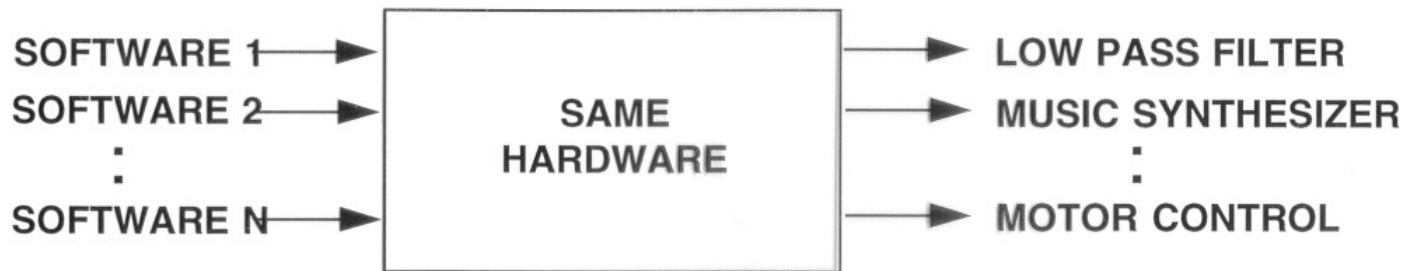
niektoré aplikácie je možné realizovať len digitálne

Lepšia časová a teplotná stabilita
dva rovnaké DSP systémy vykazujú viac rovnaké parametre

PROGRAMMABILITY

- ONE HARDWARE = MANY TASKS

Jedna schéma zapojenia - rôzne funkcie, závislé od programu



- UPGRADABILITY AND FLEXIBILITY

Pridanie funkcií a prispôsobivosť znamená:

- DEVELOP NEW CODE → UPGRADE
- ANALOGUE → SOLDER NEW COMPONENT

Číslicové sprac. - modifikovať program (do určitého stupňa nie je potrebné modifikovať zapojenie)

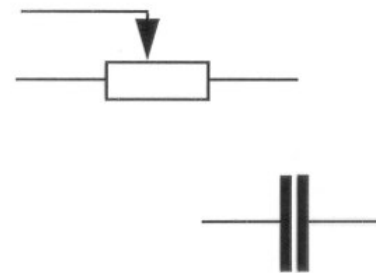
Analógové sprac. - modifikovať zapojenie

STABILITY AND REPEATABILITY

- ANALOGUE CIRCUITS ARE AFFECTED BY

- TEMPERATURE
- AGING

Na vlastnosti analógových obvodov vplýva teplota a starnutie súčiastok



- TOLERANCE OF COMPONENTS

- TWO ANALOGUE SYSTEMS
 - USING SAME DESIGN
 - USING SAME COMPONENTS
 - MAY DIFFER IN PERFORMANCE

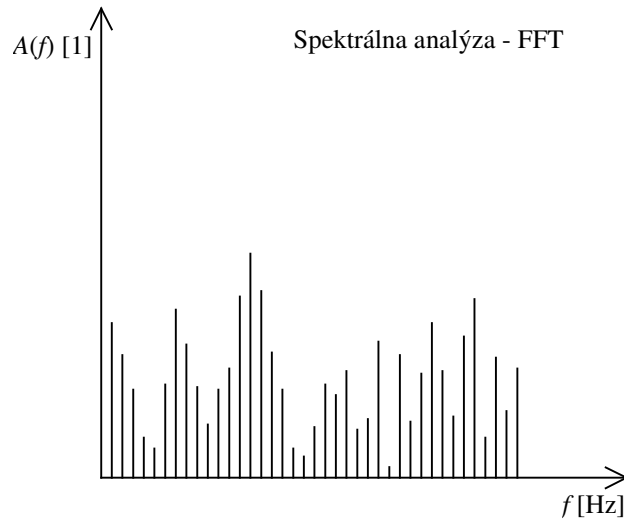
Rozptyl hodnôt súčiastok môže spôsobiť, že dve rovnaké zapojenia s rovnakými súčiastkami nemusia vykazovať rovnaké vlastnosti

PERFORMANCE

- SOME SPECIAL FUNCTIONS CAN ONLY BE IMPLEMENTED DIGITALLY Niektoré druhy spracovania signálov je možné realizovať iba číslicovo

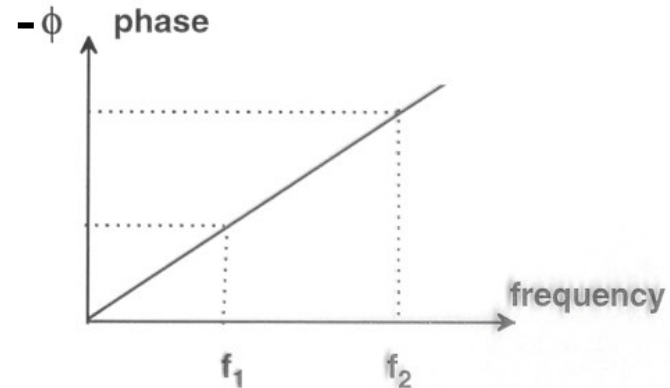
- LOSSLESS COMPRESSION

Bezstratová a stratová kompresia zvukového a obrazového signálu - MPEG, ATRAC...



- LINEAR PHASE FILTERS

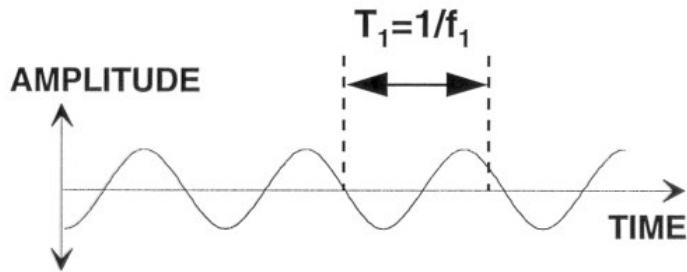
Filtre s lineárnou fázovo - frekvenčnou charakteristikou



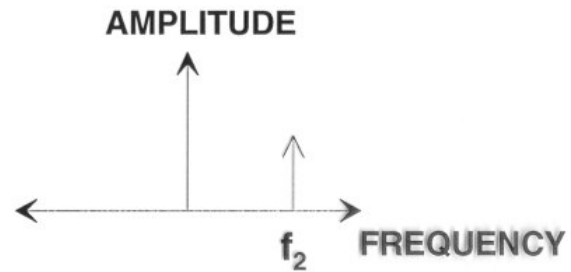
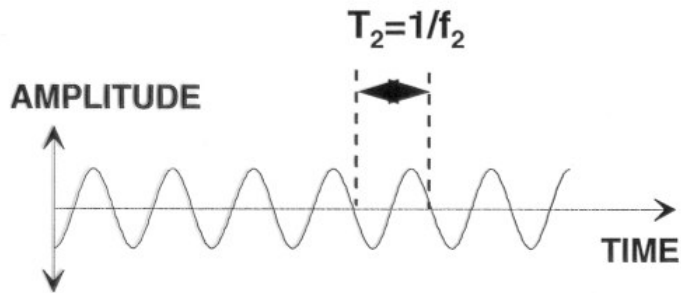
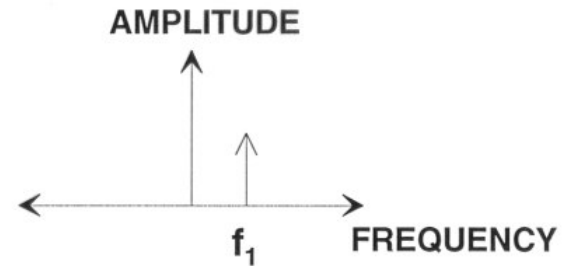
SIGNALS IN TIME AND FREQUENCY DOMAINS

Signály v časovej a frekvenčnej oblasti

TIME DOMAIN



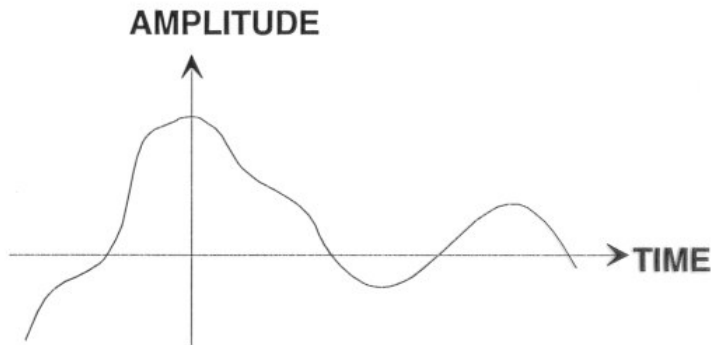
FREQUENCY DOMAIN



T = period f = frequency

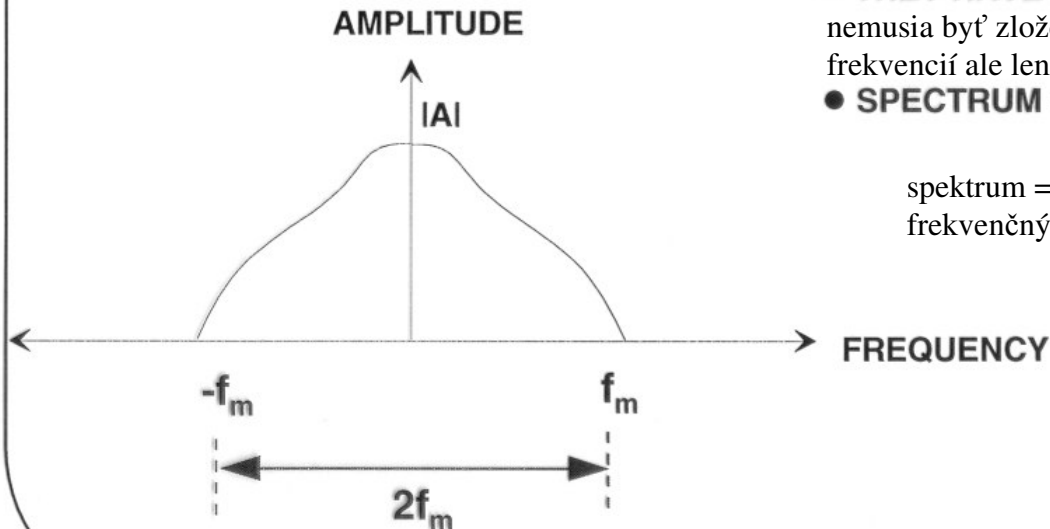
REAL SIGNALS

Reálne, všeobecné signály



Reálne, všeobecné signály sú zložené z mnohých harmonických signálov s rôznymi frekvenciami - frekvenčné zložky signálu

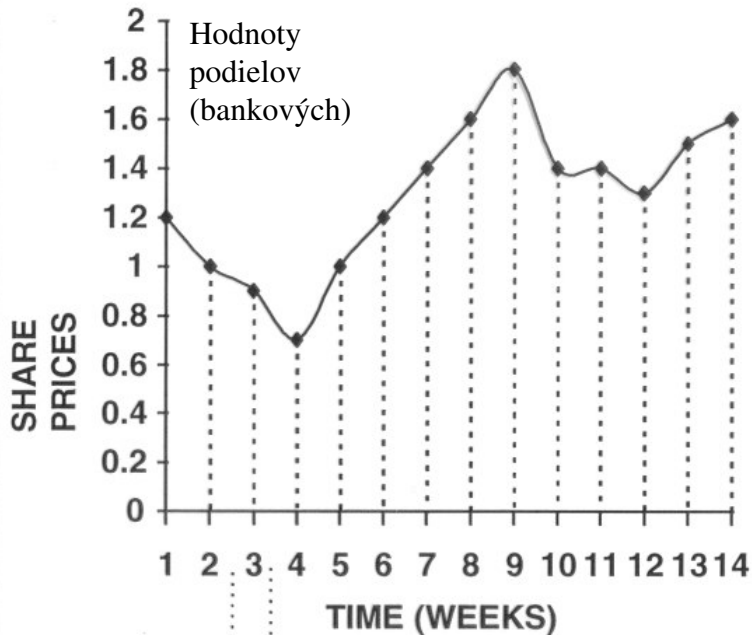
- REAL LIFE SIGNALS ARE A COMBINATION OF MANY FREQUENCIES



- THEY HAVE BANDWIDTH $2f_m$
nemusia byť zložené z harm. signálov všetkých frekvencií ale len z frekvencií z intervalu $\langle 0;f_m \rangle$
- SPECTRUM = FREQUENCY CONTENT

spektrum = zastúpenie jednotlivých frekvenčných zložiek

SAMPLING vzorkovanie



- **TAKE SNAPSHOTS OF CONTINUOUSLY CHANGING DATA**

urob fotky spojito sa meniacich hodnôt

- **'SAMPLING PERIOD' IS FIXED**

čas medzi dvoma „foteniami“ sa nazýva vzorkovacia perióda, má konštantnú hodnotu

- **THIS MAKES INFORMATION UNDERSTANDABLE**

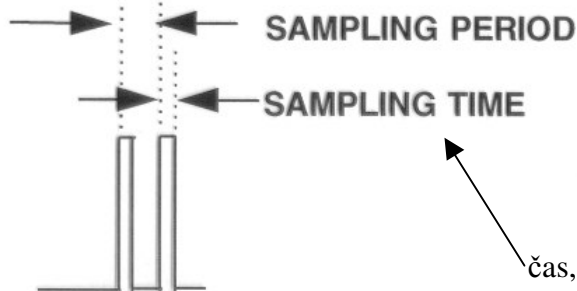
u týmto sa informácia stáva zmysluplnou (?)

- **MY SHARE PRICE HIT ITS LOWEST IN WEEK 4**

hodnota mojich podielov dosiahla minimum vo štvrtom týždni

- **MY SHARE PRICE REACHED ITS PEAK IN WEEK 9**

hodnota mojich podielov dosiahla maximum v deviatom týždni

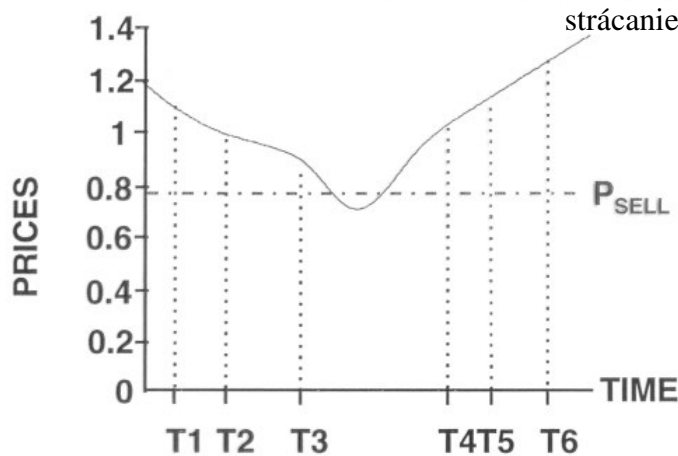


- **SAMPLING PERIOD IS THE TIME BETWEEN SAMPLES**

- **SAMPLING TIME IS THE TIME TAKEN TO TAKE A SAMPLE, 'A SNAPSHOT'**

čas, ktorý je potrebný na „odfotenie“ hodnoty

MISSING INFORMATION



strácanie informácie

● **NON-PERIODIC SNAPSHOTS**

nepravidelné „fotenie“

● **MAY MISS INFORMATION**

môže dôjsť ku strate hodnoty

THE DIP IN PRICES BETWEEN T3&T4 GOES UNNOTICED

krátky pokles v hodnote medzi okamihmi T3 a T4 sa nezaznamenal

● **INFORMATION CANNOT BE INTERPRETED EASILY**

Informácia nemôže byť správne pochopená

● **PERIODIC SNAPSHOTS**

pravidelné „fotenie“

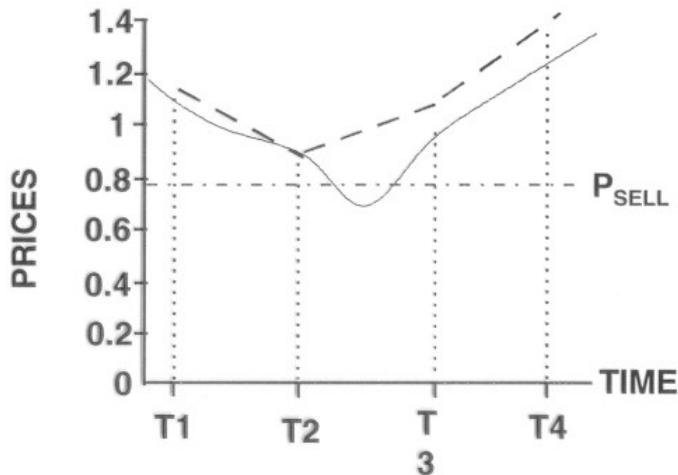
● **EASIER TO INTERPRET**

Informácia môže byť lepšie pochopená

● **MAY STILL MISS INFORMATION**

stále ale môže dôjsť ku strate informácie

● **THE KEY IS THE SAMPLING FREQUENCY**



— Actual variation
- - Inferred plot

skutočný vývoj hodnoty

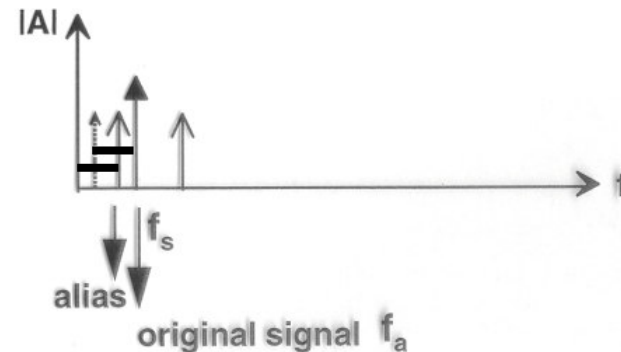
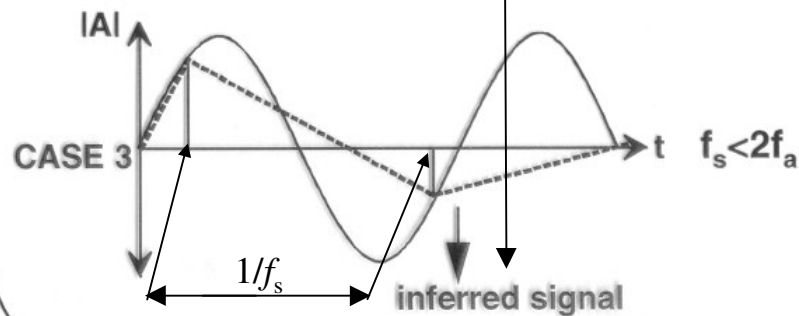
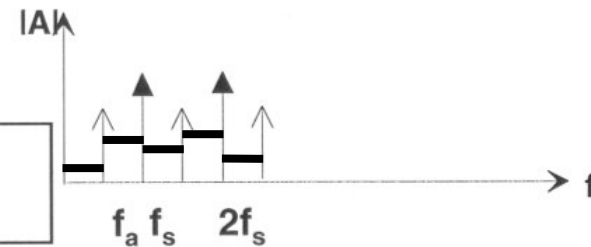
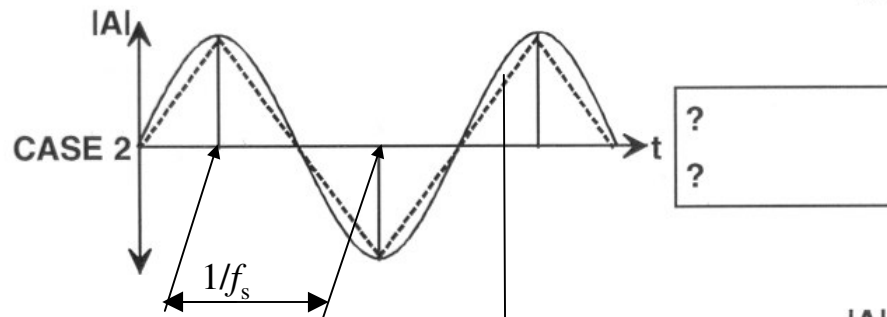
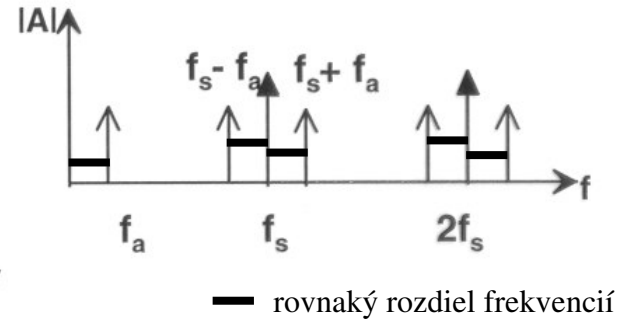
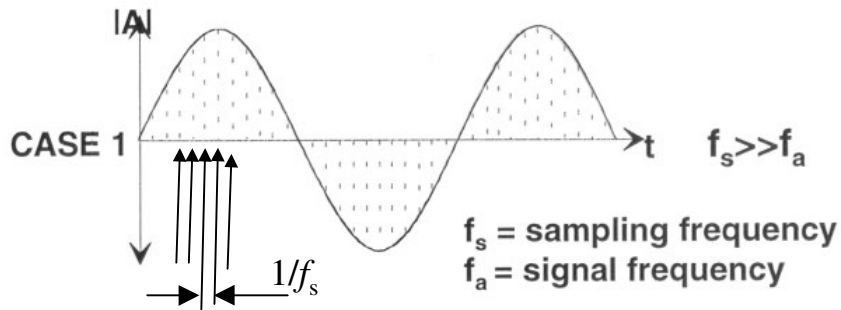
vývoj hodnoty signálu, jeho rekonštrukcia, ak poznáme jeho hodnoty iba v okamihoch T1 až T4

GETTING THE SAMPLING RIGHT

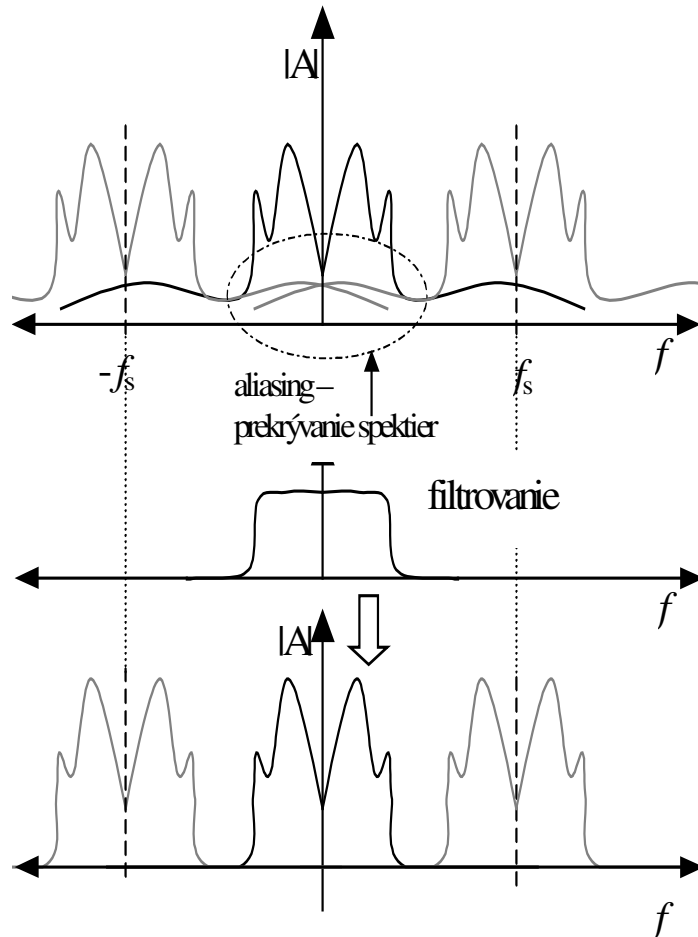
TIME

ako správne vzorkovať

FREQUENCY



LIMITING THE SPECTRUM



- SIGNALS IN THE REAL WORLD CONTAIN MANY FREQUENCIES

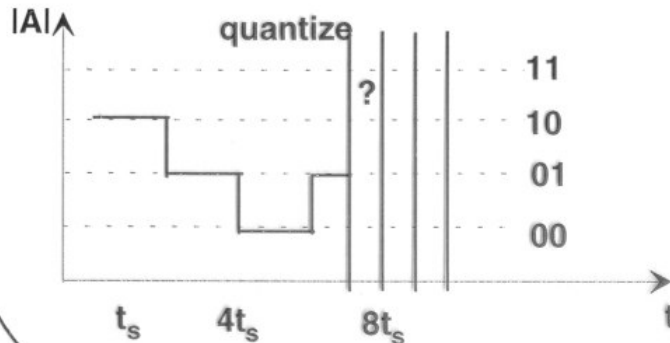
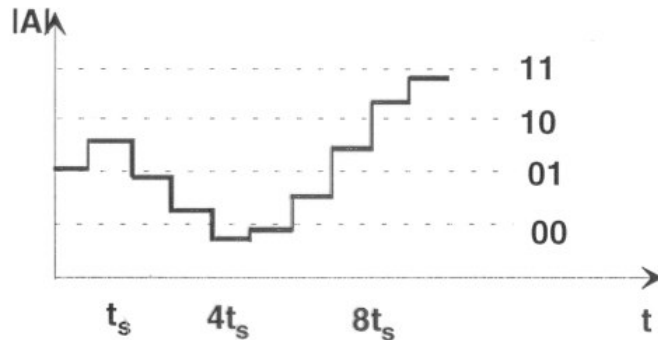
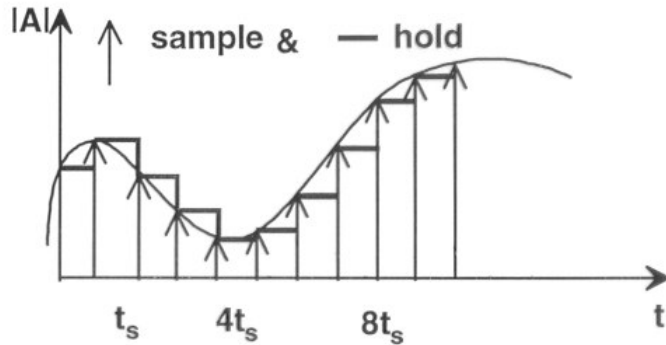
- FREQUENCY COMPONENTS GREATER THAN $1/2 f_s$ CAUSE ALIASING ($f > f_m$)
frekvencie vyššie ako $f_s/2$ spôsobujú aliasing

- GET RID OF (=FILTER OUT) FREQUENCIES ABOVE f_m
ako sa ich zbaviť - odfiltrovať ich

- THEN ENSURE SAMPLING RATE IS GREATER THAN $2f_m$

a uistiť sa, že f_s je minimálne dvojnásobná ako je najvyššia frekvenčná zložka signálu

DIGITIZING THE SIGNAL



● AIM IS TO OBTAIN '1', '0' REPRESENTATION

● SAMPLE SIGNAL PERIODICALLY

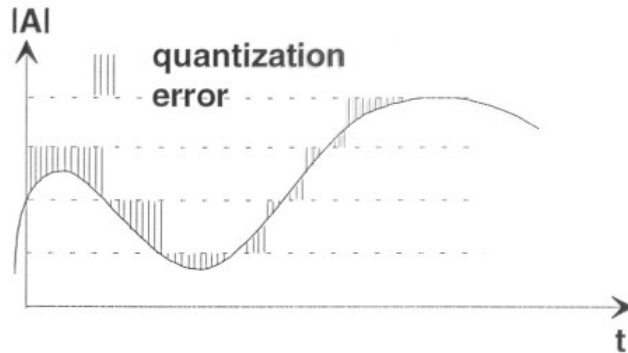
● HOLD SAMPLED VALUE UNTIL NEXT SAMPLE

● CLASSIFY NEW SIGNAL INTO LEVELS = QUANTIZE

● MORE LEVELS, MORE ACCURATE

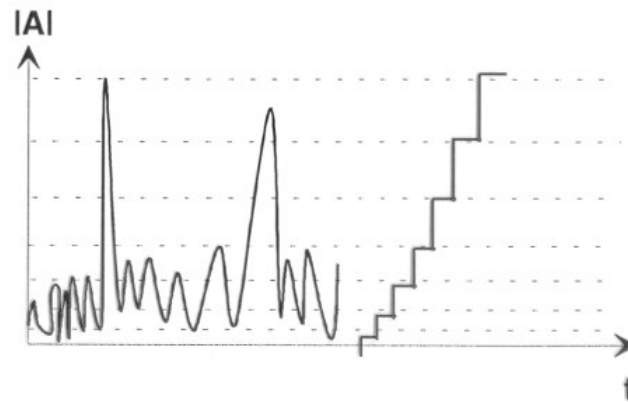
SIGNAL = 10 10 01 01 00 00 ?

QUANTIZATION ERROR



● QUANTIZATION INTRODUCES ERRORS

● INCREASING THE NUMBER OF QUANTIZATION LEVELS IS NOT ALWAYS THE ANSWER



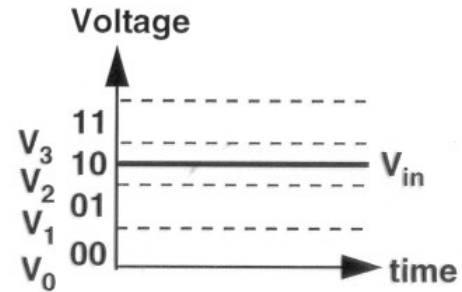
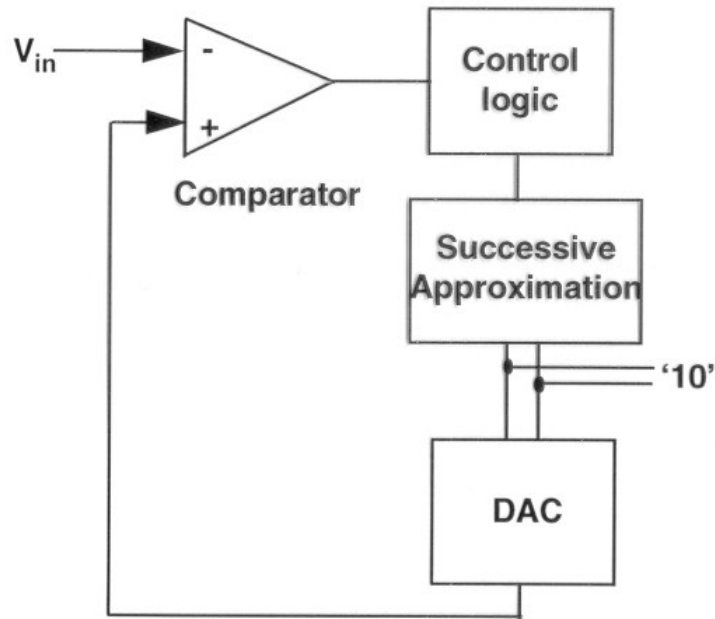
● NON-UNIFORM QUANTIZATION

● USE MORE LEVELS WHERE THERE ARE MORE VARIATIONS

● USE FEWER LEVELS WHERE THERE IS NOT MUCH CHANGE

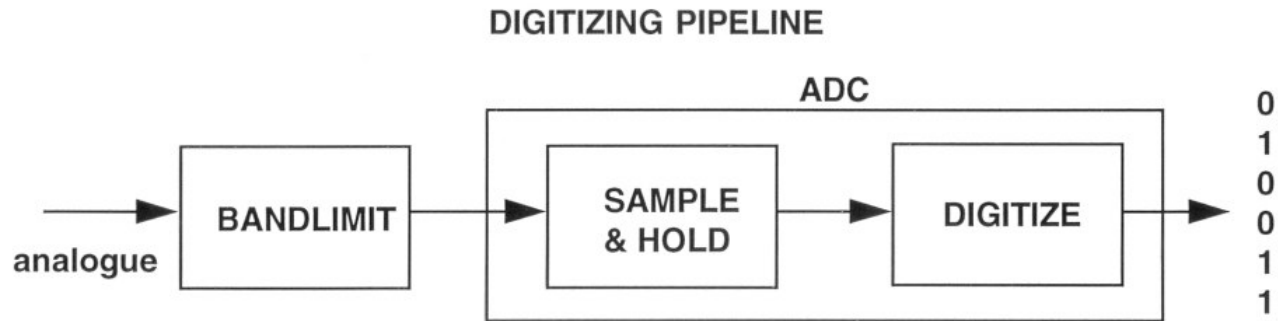
ADC CONVERTERS

SUCCESSIVE APPROXIMATION ADC



- SET DAC OUTPUT TO $V_2 = '01'$
- DAC GENERATES ANALOGUE VOLTAGE V_2
 $V_{in} > V_2$
- SET MSB TO '1'
- DAC NOW GENERATES V_3
- SET LSB TO '0' SINCE $V_3 > V_{in}$
- DIGITIZE IN TWO CYCLES
- n BITS = n CYCLES

DIFFERENT TYPES OF ADC

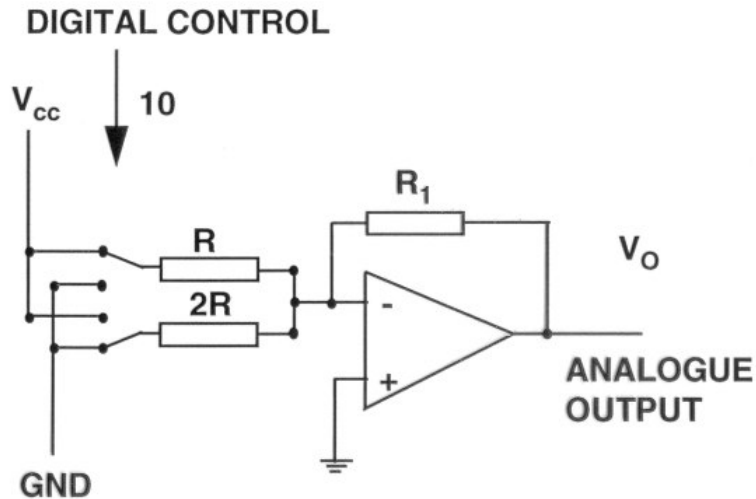


- **DUAL SLOPE ADC**
SLOW
EXPENSIVE
- **FLASH ADC**
REQUIRES PRECISION COMPONENTS
- **SIGMA DELTA ADC**
USES MOSTLY DIGITAL TECHNOLOGY
RELIABLE
STABLE

FROM DIGITAL TO ANALOGUE

- FOR '10' DIGITAL CONTROL
SWITCH IN R TO SUPPLY (V_{CC})
2R TO GROUND (GND)
ANALOGUE OUTPUT = $(R1/R) * V_{CC}$

VOLTAGE SOURCE MULTIPLYING DAC



- GAIN = $R1/\text{INPUT RESISTANCE}$
THE OUTPUT

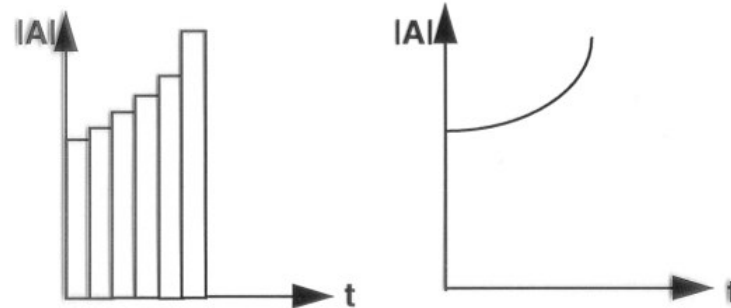
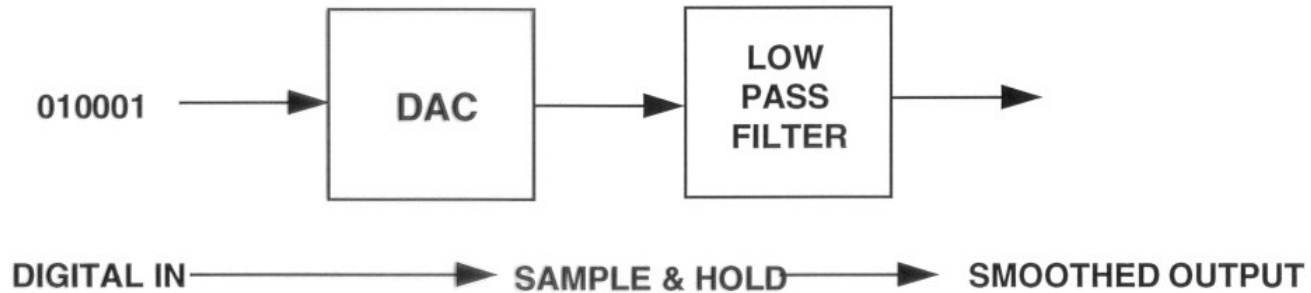
$$V_O = - \left[\underbrace{V_{in} * (R_1/R)}_{\text{MSB}} + \underbrace{V_{in} * (R_1/2R)}_{\text{LSB}} \right]$$

MSB = MOST SIGNIFICANT BIT
LSB = LEAST SIGNIFICANT BIT

- POSSIBLE INPUTS AND OUTPUTS FOR $R1 = R$

INPUTS	OUTPUTS
11	$1.5 V_{CC}$
10	V_{CC}
01	$0.5 V_{CC}$
00	0

SMOOTHING THE OUTPUT

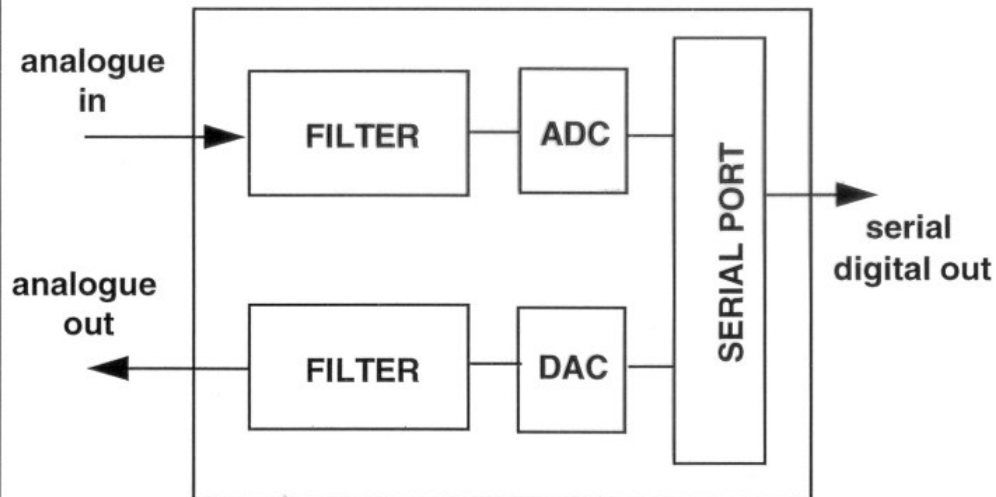


- CONVERT DIGITAL INPUT TO ANALOGUE VALUE
- HOLD UNTIL NEXT DIGITAL INPUT IS CONVERTED
- FINALLY SMOOTH THE OUTPUT SIGNAL

COMMERCIAL CONVERTERS

TLC32040

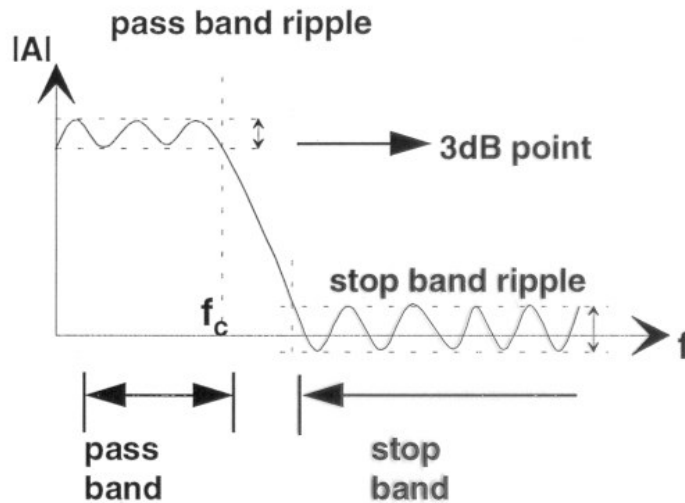
ANALOGUE INTERFACE CIRCUIT (AIC)



- ADC AND DAC ON SAME CHIP
- DIGITIZED DATA SERIALIZED
- INTERFACES TO SERIAL PORT OF DSP
- ANTI-ALIASING FILTER
- SMOOTHING FILTER
- PROGRAMMABLE FILTERS

PERFORMANCE CRITERIA

AMPLITUDE RESPONSE



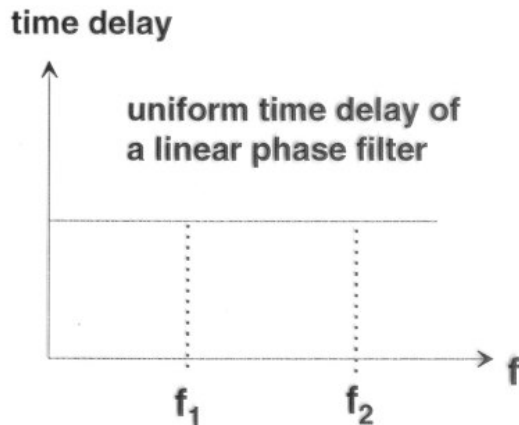
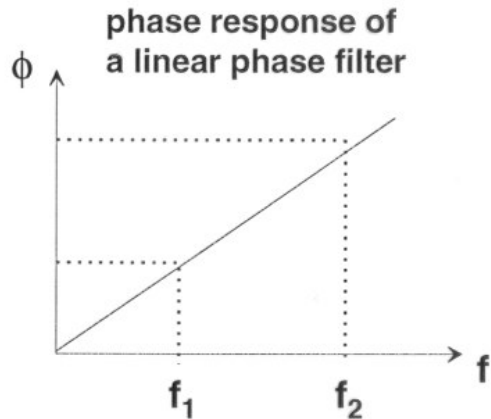
$$20 \log_{10} |A| = \text{gain in dB}$$

$f_c =$ cut off frequency

$$\text{GAIN AT 3dB point) (at } f_c) = \frac{|A|}{\sqrt{2}}$$

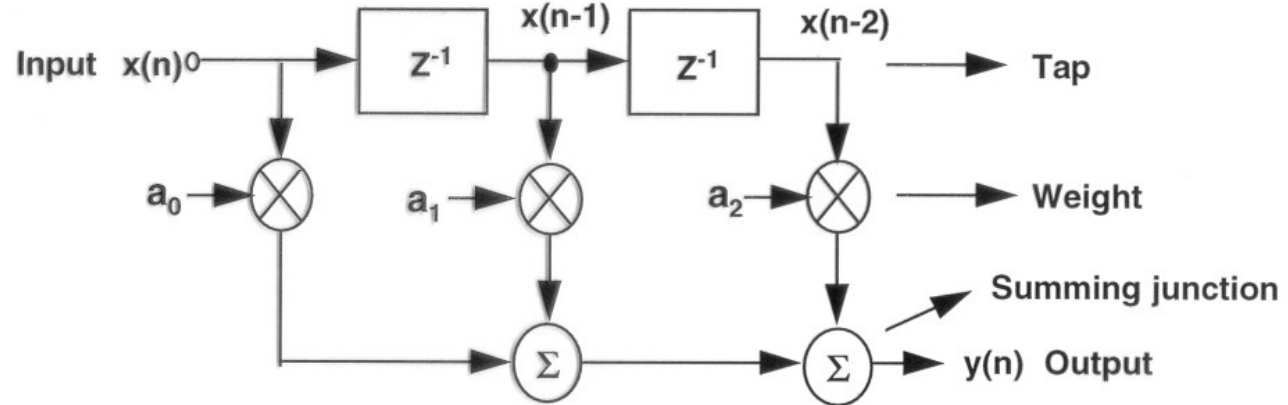
- RIPPLE IN PASS BAND CAUSES
 - NON-LINEARITY
- POSSIBLE TO DESIGN WITH NO RIPPLE
- RIPPLE IN STOP BAND IS LESS IMPORTANT
- FALL OFF dB / Decade (Gain in dB / Decade of f)
- STOP BAND ATTENUATES (SAY - 40dB)

PHASE RESPONSE



- PHASE RESPONSE REPRESENTS TIME DELAY OF DIFFERENT FREQUENCIES
- LINEAR PHASE RESPONSE DELAYS ALL FREQUENCIES BY SAME AMOUNT
TIME DELAYS AT f_1 & f_2 ARE EQUAL
- NON-LINEAR PHASE RESPONSE
 - DELAYS ALL FREQUENCIES BY DIFFERENT AMOUNTS
 - CAUSING DISTORTION TO ORIGINAL SIGNAL
 - IN A MUSIC APPLICATION WE CAN HEAR IT
 - IN A VIDEO APPLICATION WE CAN SEE IT
- LINEAR PHASE IS ONLY IMPORTANT IN PASS BAND
- A LITTLE NON-LINEARITY MAY BE TOLERATED

DIGITAL FILTERS



$x(n)$ sampled analogue waveform, $x(0)$ at $t = 0$, $x(1)$ at $t = t_s$, $x(2)$ at $t = 2 t_s \dots$

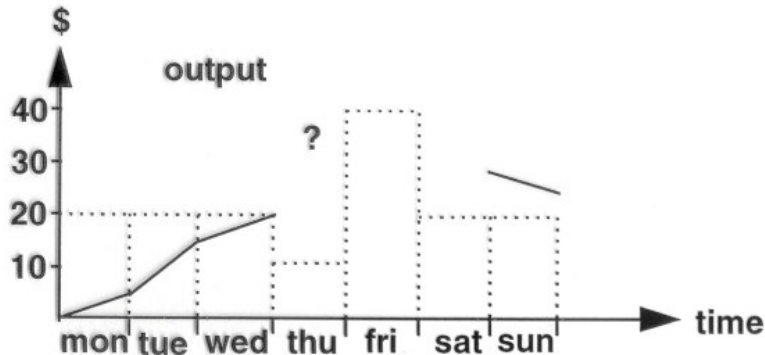
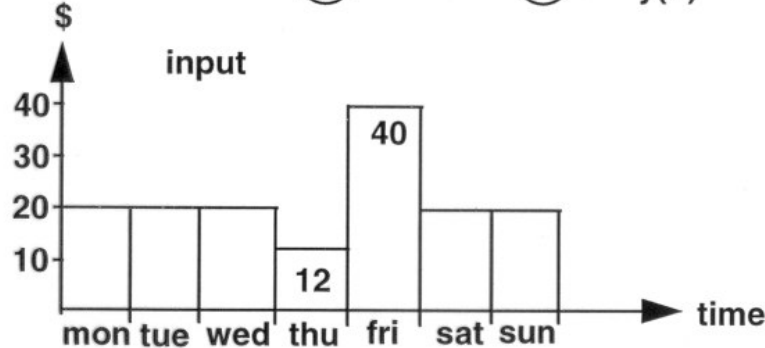
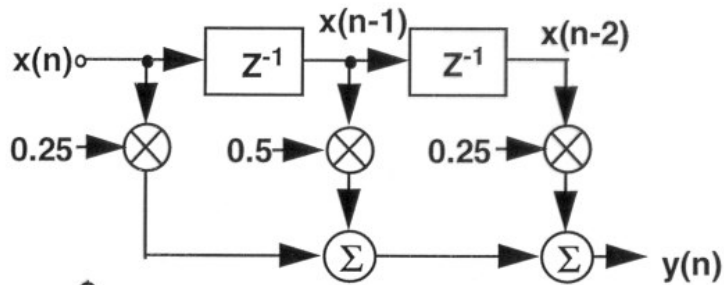
t_s is sampling period, $f_s = \boxed{?}$

a_n = weights (coefficients, scaling factor)

Z^{-1} unit time delay = one sampling period

$$y(n) = a_0 x(n) + a_1 x(n-1) + a_2 x(n-2)$$

MOVING AVERAGE FILTER



● ASSUME NO PREVIOUS INPUTS
 $X(0) = 20; X(-1) = 0; X(-2) = 0$

● AND LET

$$a_0 = 0.25 \quad a_1 = 0.5 \quad a_2 = 0.25$$

$$y(0) = 0.25x(0) + 0.5x(-1) + 0.25x(-2) = 5$$

$$y(1) = 0.25*20 + 0.5*20 + 0.25*0 = 15$$

$$y(2) = 0.25*20 + 0.5*20 + 0.25*20 = 20$$

$$y(3) = 0.25* \square + 0.5* \square + 0.25* \square = \square$$

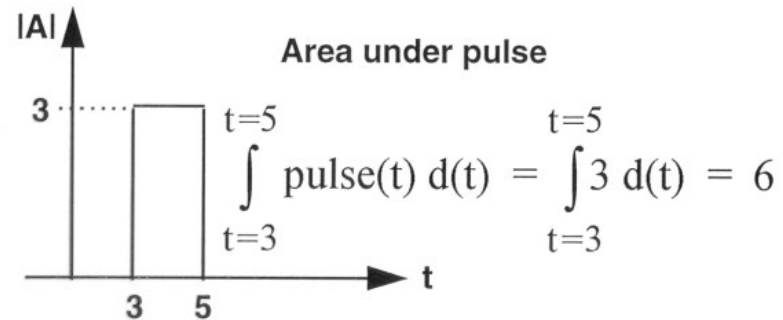
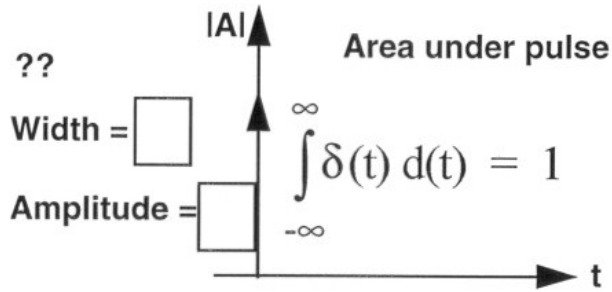
$$y(4) = 0.25* \square + 0.5* \square + 0.25* \square = \square$$

$$y(5) = 0.25*20 + 0.5*40 + 0.25*12 = 28$$

$$y(6) = 0.25*20 + 0.5*20 + 0.25*40 = 25$$

● MOVING AVERAGE CALCULATION

WEIGHTED IMPULSE FUNCTION

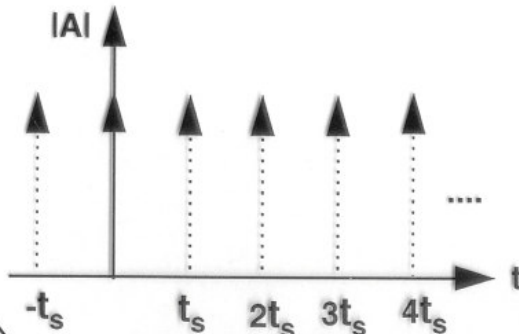


WEIGHTED IMPULSE FUNCTION

$$\int_{-\infty}^{\infty} A\delta(t) d(t) = A$$

Area = A Amplitude = ∞

SAMPLING WAVEFORM AS WEIGHTED IMPULSE TRAIN

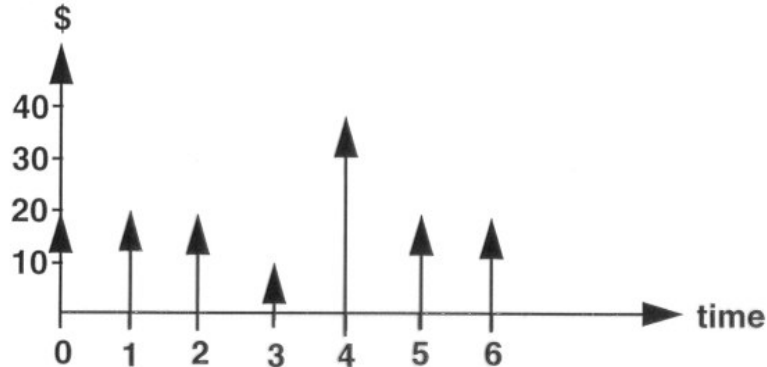


$$s(t) = \delta(t - \infty) + \dots + \delta(t - t_s) + \delta(t) + \delta(t + t_s) + \dots + \delta(t + \infty)$$

$$s(t) = \sum_{n=-\infty}^{\infty} \delta(t - nt_s)$$

FILTER FUNCTIONS

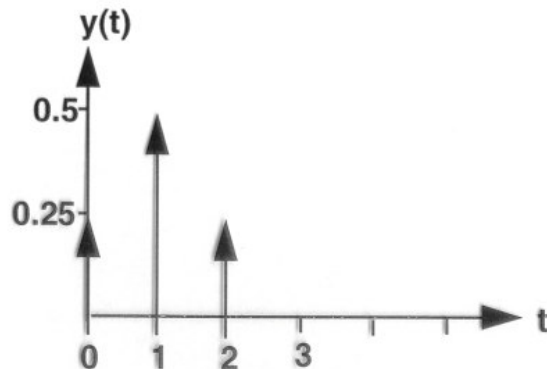
FILTER INPUT AS WEIGHTED IMPULSES



MONDAY'S INPUT VALUE

$$\int_{-\infty}^{\infty} 20 \delta(t) dt = 20$$

IMPULSE RESPONSE OF FILTER



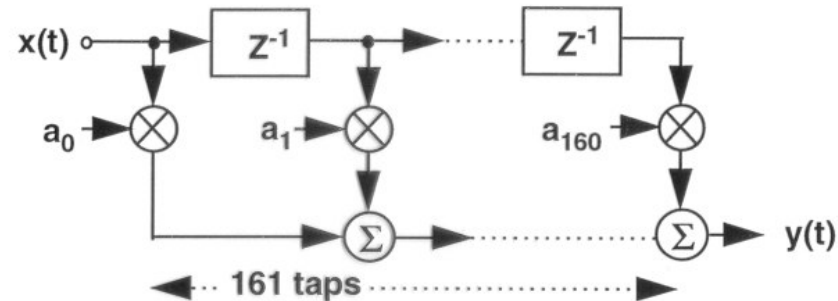
- OUTPUT WAVEFORM OBTAINED FOR A SINGLE UNITY WEIGHTED IMPULSE APPLIED AT $t = 0$

- IMPULSE RESPONSE CONSIST OF FINITE NUMBER OF PULSES HENCE FINITE IMPULSE RESPONSE (FIR) FILTER

- IMPULSE RESPONSE MAY BE USED TO OBTAIN RESPONSE TO ANY INPUT

FIR FILTERS

- A FIR FILTER WITH A STEEPER ROLL- OFF



- A MORE REALISTIC FILTER
DESIGNED USING A SOFTWARE FILTER DESIGN PACKAGE

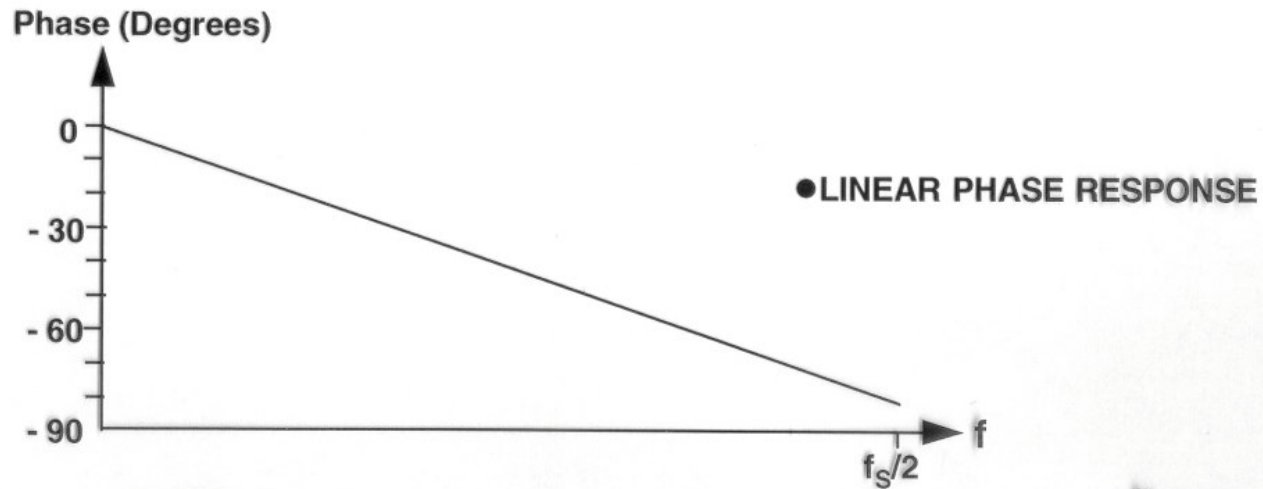
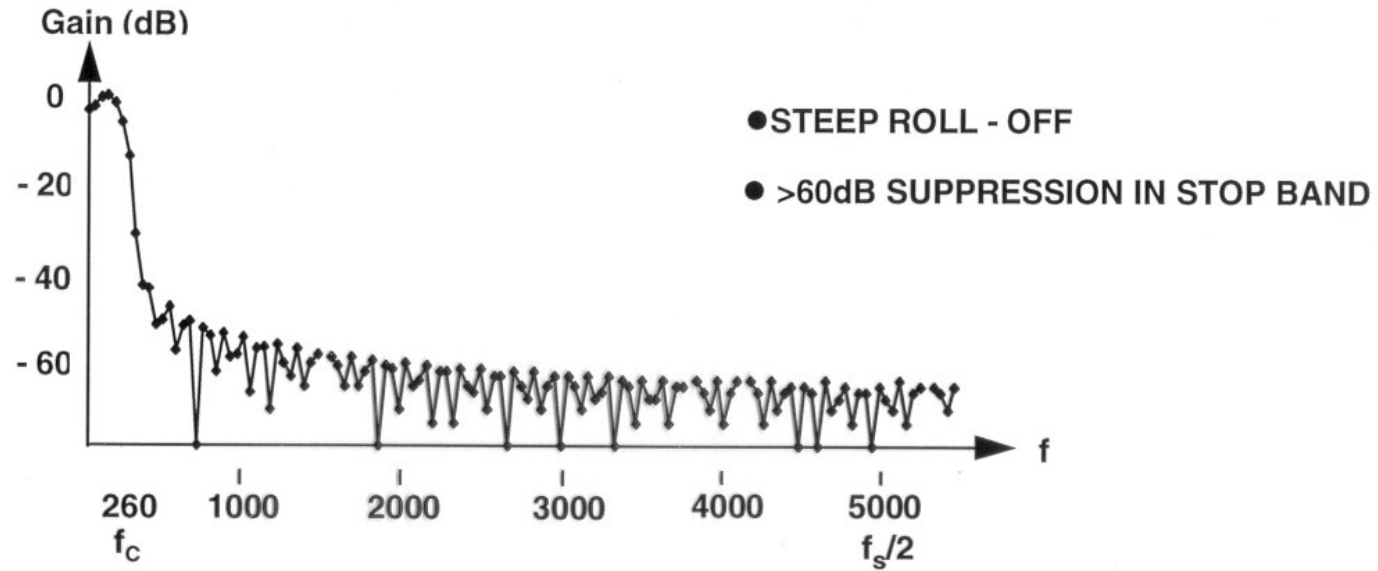
- SPECIFICATIONS:

- CUT - OFF FREQUENCY = 260 Hz
- STOP BAND ATTENUATION > 60db
- ROLL - OFF 55dB per 100Hz (VERY SHARP)

- FILTER WITH 161 TAPS
- 161 DIFFERENT GAIN VALUES

- THIS FILTER IS USED IN OUR DEMONSTRATION

FIR RESPONSE



DSP AND DIGITAL FILTERS

ANOTHER TYPE OF DIGITAL FILTER

- INFINITE IMPULSE RESPONSE (IIR) FILTER
 - DELAYS AND WEIGHTS ARE IN FEEDBACK LOOP
 - NON-LINEAR PHASE RESPONSE
 - LESS TAPS, SHARPER FALL OFF
 - MAY BE UNSTABLE

ADVANTAGES OF DIGITAL FILTERS

- PROGRAMMABLE
 - CHANGE COEFFICIENTS = NEW FILTER
- POSSIBLE TO IMPLEMENT 'ADAPTIVE' FILTERS
 - CHANGE COEFFICIENTS UNDER CERTAIN CONDITIONS ON THE FLY

WHY USE DSP FOR DIGITAL FILTER IMPLEMENTATION?

REMEMBER $A = B * C + D$

$$y(n) = a_0 x(n) + a_1 x(n-1) + a_2 x(n-2)$$

PERFORMANCE ISSUES

NOISE IN DIGITAL FILTERS

- **SIGNAL QUANTIZATION**

NOISE INTRODUCED IS PROPORTIONAL TO THE NUMBER OF BITS CONVERSION USES

- **COEFFICIENT QUANTIZATION**

COEFFICIENTS DETERMINE THE BEHAVIOUR OF FILTERS
MORE SIGNIFICANT IN IIR

- **TRUNCATION**

$0.64 \times 0.73 = 0.4672$ TRUNCATE TO 0.46

DOUBLE WIDTH PRODUCT REGISTERS AND ACCUMULATORS HELP REDUCE TRUNCATION ERRORS

- **INTERNAL OVERFLOW**

$0010 + 1111 = 10001$ → SATURATE 1111
└→ OVERFLOW

- **DYNAMIC RANGE CONSTRAINTS**

16 bit → $20 \log_{10} (2^{16}) = 96\text{dB}$

32 bit → $20 \log_{10} (2^{32}) = 192\text{dB}$